

On the Probability of any Individual being infected by HIV/Aids in a Year

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Abstract:

In this work, sexual activities of the susceptible population is taken into consideration. It is believed that each sexually active individual has sexual intercourse with at least a partner for at least once in a year. The probabilities of getting infected with the disease by sex was obtained given the same sexual behaviour.

.Keywords Sexual Behaviour, Susceptible Population, Infection, Probability, Transmission

1. Introduction

Sexual intercourse of the most vulnerable means of the spread of HIV/AIDS. This is because the likelihood is 1 that there will be at least one act of sexual intercourse every hour and this is the more reason why the mode of transmission of HIV/AIDS is highly probable through sex. According to the statistical fact sheet published by WHO (World Health Organization), the likelihood of a male contracting the disease is 0.2 and that of a female as 0.8.

The spread of HIV/AIDS through sex depends on the number of sexual partnerships, the number of acts of intercourse per partnership as well as the likelihood of transmission in a single act of sex. It also depends on the probability that a randomly selected partner is HIV positive.

2. Materials and Methods

Let individuals have m sexual partnerships per annum, and that the average number of acts of intercourse per partnership is n . Furthermore, assume that the probability of transmission in a single act of sex is β , and the HIV positive is P (the endemic prevalence). Then the probability that any sexually active individual being HIV positive in a year based on the multiplication rule of probability can be obtained as follows:

$P_y = 1 - P_y^1$ (P_y^1 is the probability of not getting infected in a year) = $1 - [P_y^1$ is the probability of not getting infected in a year]^m

$P_y = 1 - [($ Probability that a randomly selected partner is HIV positive *

(Probability of not getting infected by an HIV positive partner)ⁿ + the probability that randomly selected partner is HIV negative]^m

Therefore,

$$P_y = 1 - [P(1 - \beta)^n + (1 - P)]^m$$

P_y = probability of an individual becoming HIV positive in a year

m = number of sexual partnerships per annum

n = number of acts of intercourse per partnership

β = the probability of transmission in a single act of sex.

P = the probability that a randomly selected individual is HIV positive.

3. Results and Discussion

According to the epidemiological fact sheet on HIV and AIDs, 2008, the probability of a female getting infected with the disease in a single act of sex with an infected male is 0.8 and that of the male is 0.2.

From the data of HIV/AIDS prevalence in Nigeria, the endemic prevalence P is

$$P = \frac{2,714,000}{40,900,000} = 0.06$$

and with $\beta = (0.8, 0.2)$, various probabilities of infection can be obtained based on varying values of the m and n .

For example, if an uninfected male had 4 sexual partnerships in a year and 10 acts of intercourse per partner, then

$$P_y = 1 - [0.06(1 - 0.2)^{10} + (1 - 0.06)]^4$$

$$= 0.1976260023$$

Similarly, if an uninfected female had 4 sexual partnerships in a year and 10 acts of intercourse per partnership, then

$$P_y = 1 - [0.06(1 - 0.8)^{10} + (1 - 0.06)]^4 = 0.2193$$

Suppose that $m = 2$ and $n = 30$

For Male

$$P_y = 1 - [0.06(1 - 0.2)^{30} + (1 - 0.06)]^2 = 0.1163$$

For Female $P_y = 0.1164$

Also with $m = 2$ and $n = 40$

For Male

$$P_y = 1 - [0.06(1 - 0.2)^2 + (1 - 0.06)]^{40} = 0.5825$$

For Female

$$P_y = 1 - [0.06(1 - 0.8)^2 + (1 - 0.06)]^{40} = 0.9068$$

with $m = 2$ and $n = 30$

For Male $P_y = 0.4806$

For Female $P_y = 0.8313$

4. Conclusion

The results showed clearly that given the same sexual activities and under the same condition of sexual partnership, females are at a higher risk of getting infected than males. This may be due to the fact that the female reproductive opening has a longer area compared to that of male and the virus can easily be passed to them.

5. References

- [i] May R.M. and Andersan (1985): Endemic Infections in growing population. *Matt biosci*: 77:1411-156.
- [ii] Busenberg S and Hader K. P. (1990). Demographics and Epidemics *Matt Broscil* 101, 41-62.
- [iii] Sylvain Garden, Margaret Mackinnan, Sean vee and Andrew Recd (2003). Imperfect vaccination: some epidemiological and evolutionary consequences *prof R. Soc London* 270: 1129-1136.
- [iv] Inaba H., Kermack and Mc Kendrick (2001). The variable susceptibility model for infections diseases. *Japan J. Industr. Appli Matts*, 18 (2) :273-292.